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# CAT Logarithms, Surds & Indices Formulas

- “Logarithms, Surds and Indices” is one of the easiest topics in the quantitative section of the CAT exam.
- Although the number of formulas is high, the basic concepts are very simple to understand and apply.
- There are no shortcuts to remember and the scope of the questions that can be asked is very limited.
- The accuracy of answering questions from this section is very high and good students tend to score very well here.
- If  $X, Y > 0$  and  $m, n$  are rational numbers then

$$\rightarrow X^m \times X^n = X^{m+n}$$

$$\rightarrow X^0 = 1$$

$$\rightarrow \frac{X^m}{X^n} = X^{m-n}$$

$$\rightarrow (X^m)^n = X^{mn}$$

$$\rightarrow X^m \times Y^m = (X \times Y)^m$$

$$\rightarrow \frac{X^m}{Y^m} = \left(\frac{X}{Y}\right)^m$$

$$\rightarrow X^{-m} = \frac{1}{X^m}$$

- If X and Y are positive real numbers and a,b are rational numbers

$$\rightarrow \left(\frac{X}{Y}\right)^{-a} = \left(\frac{Y}{X}\right)^a$$

$$\rightarrow X^{1/a} = \sqrt[a]{X}$$

$$\rightarrow X^{a/b} = \sqrt[b]{X^a}$$

$$\rightarrow \sqrt[a]{X} \times \sqrt[a]{Y} = \sqrt[a]{XY}$$

$$\rightarrow \frac{\sqrt[a]{X}}{\sqrt[a]{Y}} = a \frac{X}{Y}$$

$$\rightarrow \frac{1}{\sqrt{N+1}-\sqrt{N}} = \sqrt{N+1} + \sqrt{N}$$

- Surds is an irrational number involving a root.

$$\text{Ex: } \sqrt{5}, \sqrt[3]{7}, \sqrt[5]{2}$$

- Like surds are two surds having the same number under radical sign.
- Like surds can be added or subtracted.

$$6\sqrt{2} + 3\sqrt{2} = 9\sqrt{2}$$

- If  $a + \sqrt{b} = c + \sqrt{d}$ , then  $a = c$  and  $b = d$ .
- The conjugate of  $a + \sqrt{b}$  is  $a - \sqrt{b}$

$$\bullet \sqrt{a\sqrt{a\sqrt{a\cdots\infty}}} = a$$

$$1 - \left[ \frac{1}{2^x} \right]$$

- To find  $\sqrt{x} + \sqrt{y}$ ,  $\sqrt{x} + \sqrt{y}$  should be written in the form of  $m + n + 2\sqrt{mn}$  where  $x = m + n$  and  $4mn = y$  and  $\sqrt{\sqrt{x} + \sqrt{y}} = \pm (\sqrt{m} + \sqrt{n})$
- If  $N = a^x$  then,  $x$  is defined as the logarithm of  $N$  to base  $a$  or  $x = \log_a N$  a logarithm of a negative number or zero is not defined
- $\log_a 1 = 0$
- $\log_a xy = \log_a x + \log_a y$
- $\log_a b^c = c \log_a b$
- $\log_a a = 1$
- $X^{\log_b y} = Y^{\log_b x}$



- $\log_a \sqrt[n]{b} = \frac{\log_a b}{n}$
  - $\log_a x = \frac{1}{\log_x a}$
  - $b^{\log_b x} = x$
  - $\log_a b = \frac{\log_c b}{\log_c a}$
  - $\log_a b * \log_b a = 1$
  - $\log_a \left(\frac{X}{Y}\right) = \log_a X - \log_a Y$
  - If  $0 < a < 1$ , then  $\log_a x < \log_a y$  (if  $x > y$ )
  - If  $a > 1$  then  $\log_a x > \log_a y$  (if  $x > y$ )
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